



Benha University

1st Term (January 2015) Final Exam

Class: 4th Year Students

Subject: Image Processing



Faculty of Computers & Informatics

Date: 10/1/2016

Time: 3 Hours

Examiner: Dr. M. Taha

Answer the following questions:

Question (1) please make a table of two columns, one for the question no. and the other for your selection

- 1) The process of moving a filter mask over the image and computing the sum of products at each location is defined by _____
a) Convolution b) Rotation c) Linearity d) **Correlation** e) None of the above
- 2) The sum of all components of a normalised histogram is equal to _____
a) Size of the image b) Size of rows of the image c) Size of columns of the image d) **One** e) $M \times N$
- 3) Image restoration usually uses a model that is based on _____
a) **Additive noise** b) Multiplicative noise c) Division noise d) Subtractive noise
e) None of the above
- 4) Convolution is usually used in the _____ domain.
a) Frequency b) **Spatial** c) Feature d) Featureless e) None of the above
- 5) Fourier transform is a _____ transform
a) **Linear** b) Nonlinear c) Bilinear d) Bicubic e) None of the above
- 6) Ideal filters can be _____
a) LPF b) HPF c) BPF d) **All of the above** e) None of the above
- 7) The Rayleigh density can be used to approximate _____
a) Ideal histograms b) Non-Ideal histograms c) Butterworth histograms d) Gaussian histograms
e) **Skewed histograms**
- 8) Which of the following filters is effective in the presence of salt-and-pepper noise?
a) Average filter b) **Median filter** c) Sobel filter d) Robert filter e) All of the above
- 9) _____ is the process of using known data to estimate values at unknown locations.
a) Decimation b) **Interpolation** c) Formulation d) All of the above e) None of the above
- 10) An image element is usually called a _____
a) **Pixel** b) $f(x,y)$ c) picture point d) All of the above e) None of the above

Question (2)

- a) For the image shown in Fig. 2(a), find a transformation function (i.e. a look-up-table) that will change its histogram to match the one shown in Table 1. Draw the transformed image in Fig. 2(b). Also determine the histogram of the transformed image. Assume that the processed images can only take integer values between 0 and 7 (including 0 and 7).

- b) Briefly explain the operation of the Alpha-trimmed mean filter. What are its uses for image processing?

where the value of d can range from 0 to $mn - 1$. When $d = 0$, the alpha-trimmed filter reduces to the arithmetic mean filter discussed in the previous section. If we choose $d = (mn - 1)/2$, the filter becomes a median filter. For other values of d , the alpha-trimmed filter is useful in situations involving multiple types of noise, such as a combination of salt-and-pepper and Gaussian noise.

Alpha-trimmed mean filter

Suppose that we delete the $d/2$ lowest and the $d/2$ highest gray-level values of $g(s, t)$ in the neighborhood S_{xy} . Let $g_r(s, t)$ represent the remaining $mn - d$ pixels. A filter formed by averaging these remaining pixels is called an *alpha-trimmed mean filter*:

$$\hat{f}(x, y) = \frac{1}{mn - d} \sum_{(s,t) \in S_{xy}} g_r(s, t)$$

Question (3)

a)

$$\text{Sobel operators: } H_x = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}; \quad H_y = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

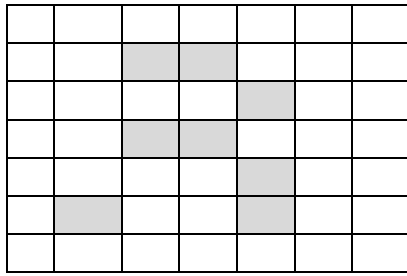
For every pixel: 1) compute vertical gradient g_x by convolving with H_x , 2) compute horizontal gradient g_y by convolving with H_y , 3) find the gradient magnitude using $A = \sqrt{g_x^2 + g_y^2}$. 4) if $A \geq T$, this pixel is an edge, otherwise, it is not an edge.

b) Write a MATLAB function that will implement these steps in (a). Assuming the image size is W (width) \times H (height). Also you can ignore the boundary problem by performing edge detection only on non-boundary pixels.

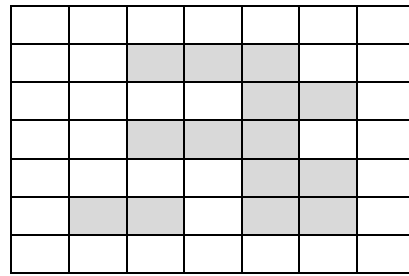
Question (4)

a) For regular (global) thresholding you find threshold value or values for the entire image. In adaptive thresholding the image is divided into part, usually square, and threshold levels are found for each separate part. Global thresholding is useful when the image is similar in most parts. Adaptive thresholding is very useful when the image is changing in intensity, e.g., because of a light source from the right side. Then the threshold values should be quite different on the left and right side of the image.

b) the opening of the binary image, F ,



F ⊖ H



(F ⊖ H) ⊕ H

c)

b) Stage A

$$A_1 = Z_{med} - Z_{min}$$

$$A_2 = Z_{med} - Z_{max}$$

if $A_1 > 0$ and $A_2 < 0$

go to Stage B

else increase window size

if window size $\leq 5 \times 5$ repeat Stage A

Else output Z_{med}

Stage B

$$B_1 = Z_{xy} - Z_{min}$$

$$B_2 = Z_{xy} - Z_{max}$$

if $B_1 > 0$ and $B_2 < 0$

output Z_{xy}

else output Z_{med}

To get Z

First with Filter of 3×3 0000 4 5 7 7

$$Z_{min} = 0 \quad Z_{max} = 7 \quad Z_{med} = 0$$

$$A_1 = 0 \quad A_2 = -7 \quad (A_1 > 0 \ \& \ A_2 < 0) \Rightarrow \text{False}$$

increase window size 5×5

0000 0003 33 33 33 33 44 4 5 6 7 7

$$Z_{min} = 0 \quad Z_{max} = 7 \quad Z_{med} = 3 \quad Z_{xy} = 0$$

$$A_1 = 3 \quad A_2 = -4 \quad A_1 > 0 \ \& \ A_2 < 0$$

$$B_1 = 0 - 0 = 0 \quad B_2 = -7 \quad B_1 > 0 \ \& \ B_2 < 0 \ \text{False}$$

output $Z_{med} = 3$

$Z = 3$

To get X → First with Filter 3×5

000 3 4 5 6 7 7
 min med max

$$A_1 = 4 \quad A_2 = -3 \quad Z_{xy} = 7$$

$$\text{Stage B} \Rightarrow B_1 = 7 \quad B_2 = 0$$

output $Z_{med} = 4$

$X = 4$

To get $y \rightarrow$ First with mask 3×3

$0003 \boxed{3} 4677$
 $z_{min} \quad z_{med} \quad z_{max}$
 $A_1 = 3 \quad A_2 = -4 \quad A_1 > 0 \ \& \ A_2 < 0 \rightarrow \text{True}$
 $B \Rightarrow z_{xy} = 0$
 $B_1 = 0 \quad B_2 = -7 \quad B_1 > 0 \ \& \ B_2 < 0 \rightarrow \text{False}$
 output $z_{med} = 3$ $y = 3$

Question (5)

A) Redundancies Types

- a) Coding Redundancy.
 Let's assume, that a discrete random variable r_k in the interval $[0, 1]$ represents the gray levels of an image and each r_k occurs with probability p_k . Where L is the number gray levels, n_k is the number of times that the k th gray level appears in image. n is the total number of pixel in the image. The average length of the code words assigned to the various gray level values where $l(r_k)$ no. of bits used to represent each gray $p(r_k)$ probability that gray level occurs
- b) Spatial and Temporal Redundancy.
 i.e. Video sequence (Correlated pixels are not repeated.)
- c) Irrelevant Information.
 Information that ignored by human visual system

b)

Coding efficiency and Huffman coding

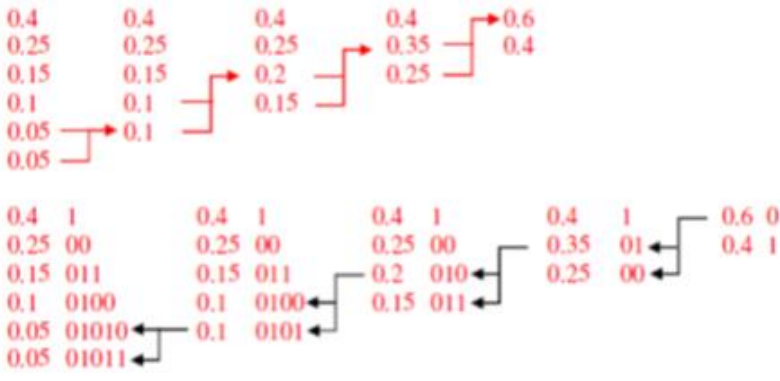
You have a source with 6 symbols $\{a_1, a_2, a_3, a_4, a_5, a_6\}$.

The probability for each symbol is $z = [0,15 \ 0,25 \ 0,05 \ 0,05 \ 0,4 \ 0,1]$.

a) Calculate the entropy of the source.

$$H(z) = -(0,15 \cdot \log_2(0,15) + 0,25 \cdot \log_2(0,25) + 0,05 \cdot \log_2(0,05) + 0,05 \cdot \log_2(0,05) + 0,4 \cdot \log_2(0,4) + 0,1 \cdot \log_2(0,1)) = 2,20$$

b) Create a Huffman code for the source.



Code = [011 00 01010 01011 1 0100]

c) Calculate the average word length of the source.

$$0,4 \cdot 1 + 0,25 \cdot 2 + 0,15 \cdot 3 + 0,1 \cdot 4 + 0,05 \cdot 5 + 0,05 \cdot 5 = 2,25$$

d) Calculate the coding efficiency for the Huffman code.

$$100 \cdot \frac{2,20}{2,25} = 97,8\%$$

GOOD LUCK